

Bestimmen Sie alle Winkel x für die gilt:

- a) $\sin(3x + 15^\circ) = -0.5$ b) $2 \cos(x - 60^\circ) = -1$ c) $\tan(4x) = \sqrt{3}$
d) $2 \sin(x + 15^\circ) = -\sqrt{2}$ e) $2 \cos(3x - 60^\circ) = 1$ f) $2 \sin(0.3x + 45^\circ) = -\sqrt{3}$
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a) $\sin(3x + 15^\circ) = -0.5$

$$\begin{aligned} 3x + 15^\circ &= -30^\circ + k \cdot 360^\circ & \text{oder} & & 3x + 15^\circ &= 210^\circ + k \cdot 360^\circ \\ &= 330^\circ + k \cdot 360^\circ & & & 3x &= 195^\circ + k \cdot 360^\circ \\ 3x &= 315^\circ + k \cdot 360^\circ & & & \mathbf{x} &= \mathbf{65^\circ + k \cdot 120^\circ} \\ \mathbf{x} &= \mathbf{105^\circ + k \cdot 120^\circ} \end{aligned}$$

Das sind im Bereich $[0^\circ; 360^\circ]$ 6 Winkel! ($65^\circ, 105^\circ, 185^\circ, 225^\circ, 305^\circ, 345^\circ$)

b) $2 \cos(x - 60^\circ) = -1$

$$\begin{aligned} \cos(x - 60^\circ) &= \frac{-1}{2} \\ x - 60^\circ &= 120^\circ + k \cdot 360^\circ & \text{oder} & & x - 60^\circ &= 240^\circ + k \cdot 360^\circ \\ \mathbf{x} &= \mathbf{180^\circ + k \cdot 360^\circ} & & & \mathbf{x} &= \mathbf{300^\circ + k \cdot 360^\circ} \end{aligned}$$

c) $\tan 4x = \sqrt{3}$

$$\begin{aligned} 4x &= 60^\circ + k \cdot 180^\circ & | : 4 \\ \mathbf{x} &= \mathbf{15^\circ + k \cdot 45^\circ} \end{aligned}$$

d) $2 \sin(x + 15^\circ) = -\sqrt{2}$

$$\begin{aligned} \sin(x + 15^\circ) &= \frac{-\sqrt{2}}{2} \\ x + 15^\circ &= 225^\circ + k \cdot 360^\circ & \text{oder} & & x + 15^\circ &= 315^\circ + k \cdot 360^\circ \\ \mathbf{x} &= \mathbf{210^\circ + k \cdot 360^\circ} & & & \mathbf{x} &= \mathbf{300^\circ + k \cdot 360^\circ} \end{aligned}$$

e) $2 \cos(3x - 60^\circ) = 1$

$$\cos(3x - 60^\circ) = 0.5$$

$$3x - 60^\circ = 60^\circ + k \cdot 360^\circ$$

$$3x = 120^\circ + k \cdot 360^\circ$$

$$\mathbf{x = 40^\circ + k \cdot 120^\circ}$$

oder $3x - 60^\circ = 300^\circ + k \cdot 360^\circ$

$$3x = 360^\circ + k \cdot 360^\circ$$

$$3x = 0^\circ + k \cdot 360^\circ$$

$$\mathbf{x = k \cdot 120^\circ}$$

f) $2 \sin(0.3x + 45^\circ) = -\sqrt{3}$

$$\sin(0.3x + 45^\circ) = -\frac{\sqrt{3}}{2}$$

$$0.3x + 45^\circ = 240^\circ + k \cdot 360^\circ$$

$$0.3x = 195^\circ + k \cdot 360^\circ$$

$$\mathbf{x = 650^\circ + k \cdot 1200^\circ}$$

oder $0.3x + 45^\circ = 300^\circ + k \cdot 360^\circ$

$$0.3x = 255^\circ + k \cdot 360^\circ$$

$$\mathbf{x = 850^\circ + k \cdot 1200^\circ}$$